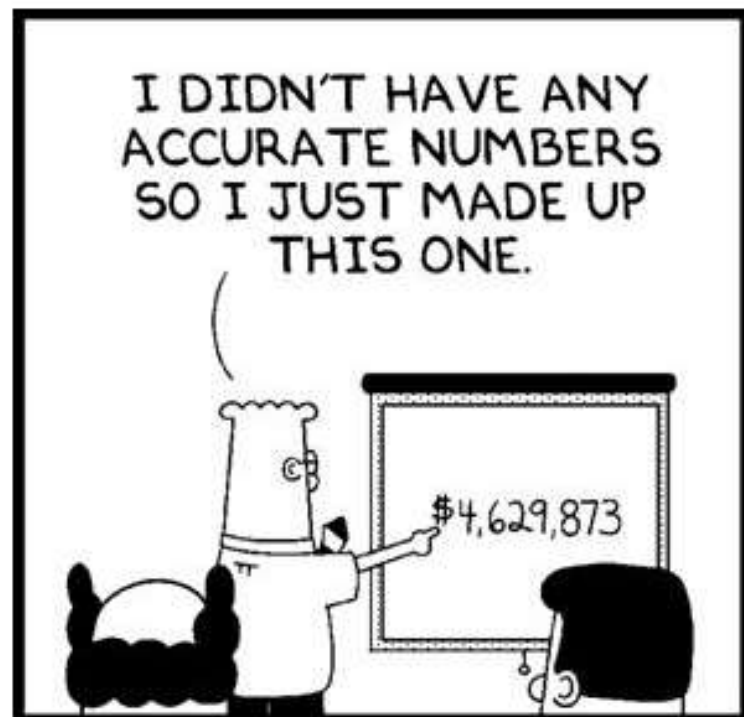


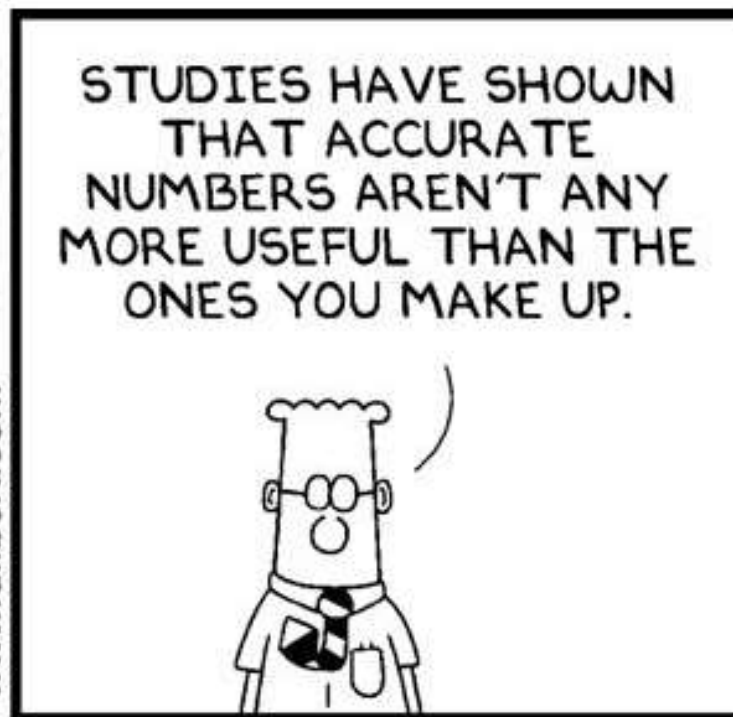
Understanding
the Effects of
Uncertainty

Garbage In = Garbage Out (GIGO)

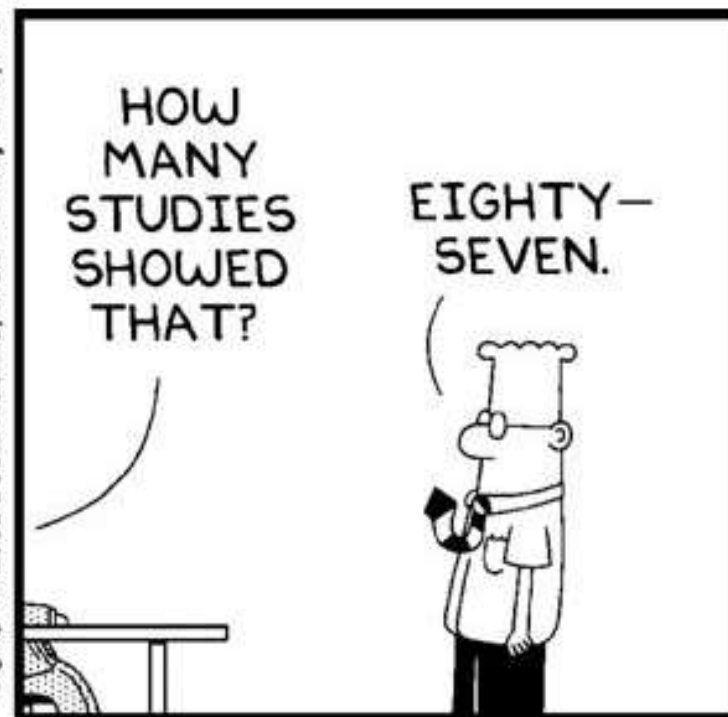
Brian Wodka
RMF Engineering
IDEA CampusEnergy 2019 – New Orleans, LA



www.dilbert.com scottadams@aol.com



5808 ©2008 Scott Adams, Inc./Dist. by UFS, Inc.



DILBERT: © Scott Adams/Dist. by United Feature Syndicate, Inc.

“Garbage in equals garbage out.”

‘Your analysis is only as good as your data.’

So... how good *is* your data?

What is the value of your analysis?

How impactful is your data/analysis on decisions?



Definition of “Uncertainty”

“The lack of being certain.”

- *Merriam-Webster*



“Measurement Uncertainty”

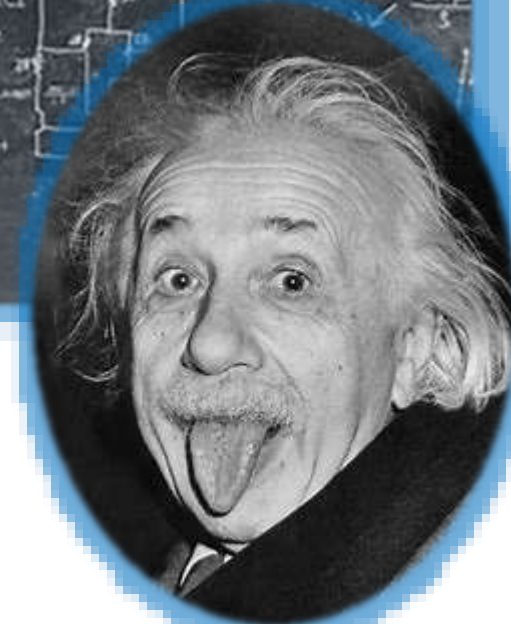
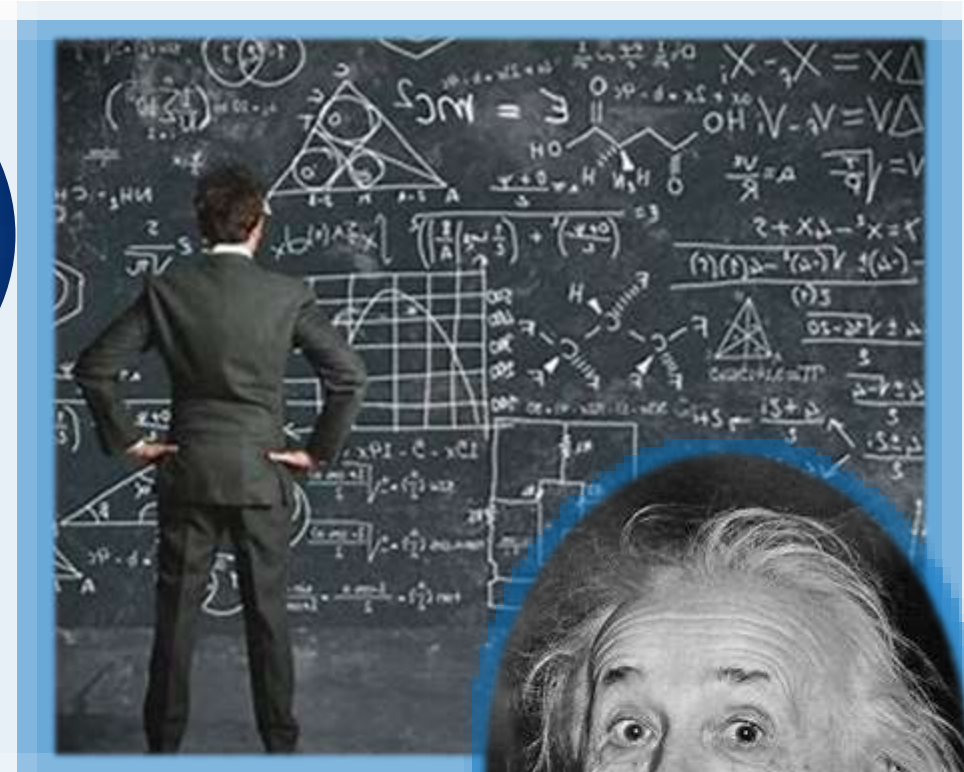
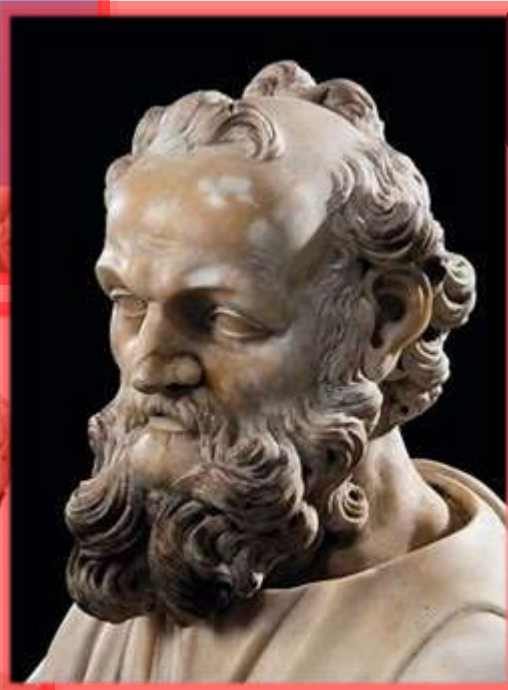
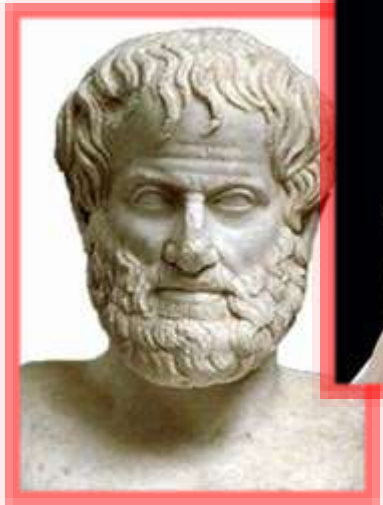
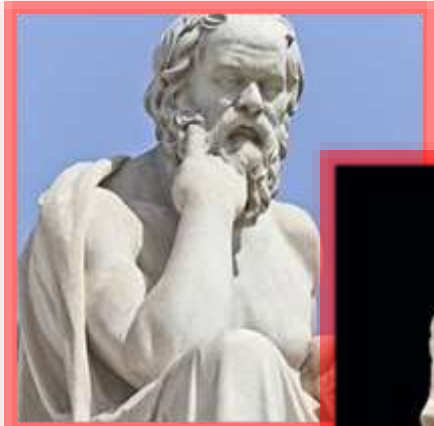
A “non-negative parameter characterizing the dispersion of the quantity values being attributed to a measurand, based on the information used.”

- *JCGM 200:2008 (VIM), definition 2.26*

Measurement Uncertainty

- Addresses the inevitable error inherent in all measurements.
- Do not define “error” as “mistake”, but instead as a known ‘variance’.
- The difference between an observed or calculated value and a true value.
- *It is used as a measure of the quality of a test.*

The Uncertainty of Uncertainty



The TRUTH
...is out there.

The Uncertainty of Uncertainty

- **“Uncertainty itself is uncertain, therefore, you cannot evaluate it exactly.”**
 - Milivoje Kostic, professor of mechanical engineering, Northern Illinois University
- **“Calibration is not perfect because you’re only comparing your instrument with something that is a little better.”**
 - W. Glenn Steele, distinguished professor of mechanical engineering, Mississippi State University
- **“Essentially, all models are wrong, but some are useful.”**
 - George E. P. Box
- **“Uncertainty is the science of accuracy of the inaccuracy of science.”**
 - Me

Accuracy and Precision

Accuracy

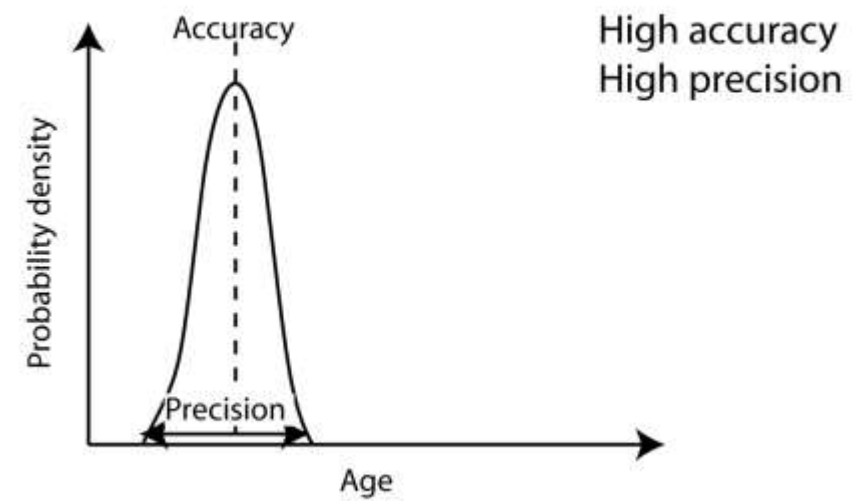
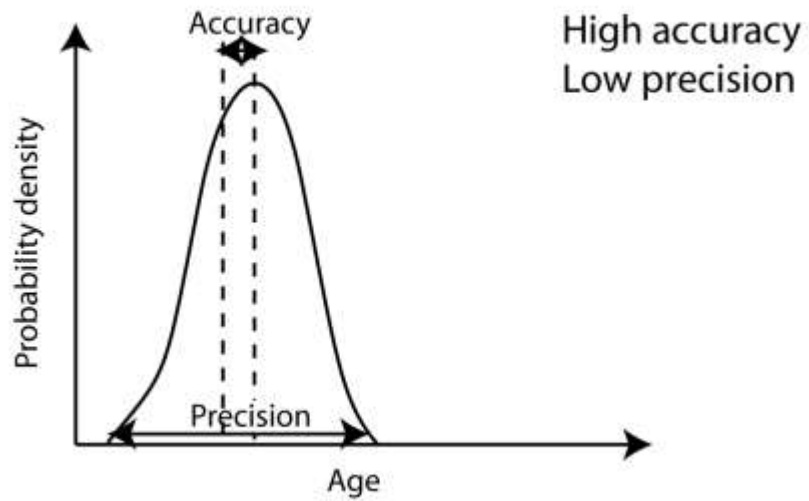
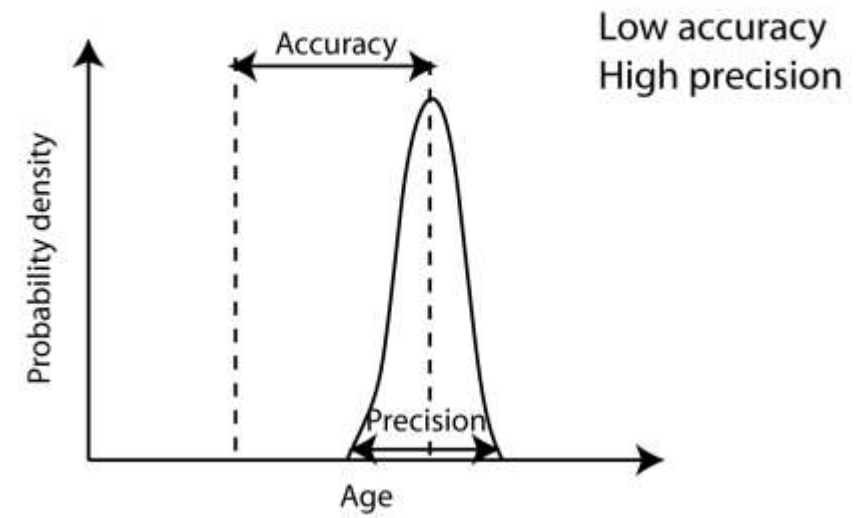
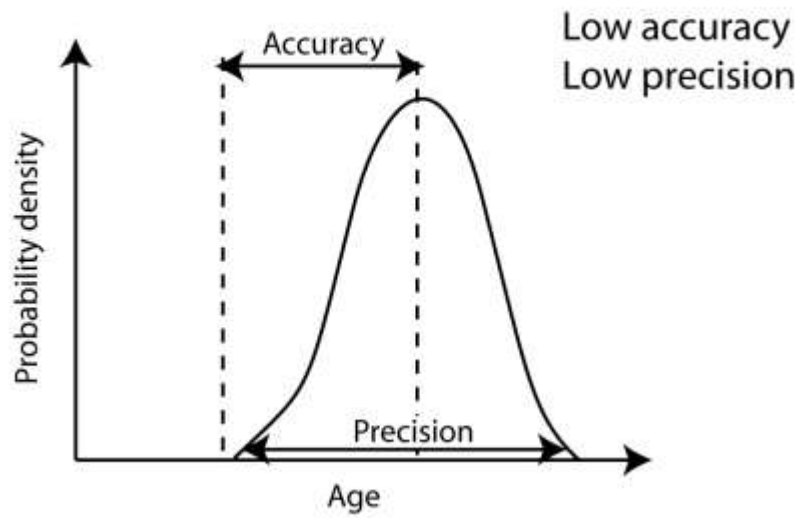
How close a measurement is to the true value

Accuracy Error: *Systematic error, Bias*

Precision

Magnitude of variation in a set of measurements

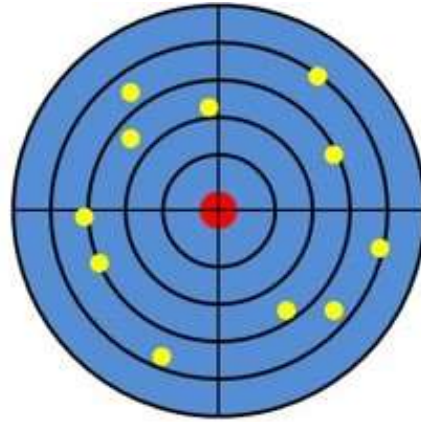
Precision Error: *Random error, Scatter*



Accuracy and Precision



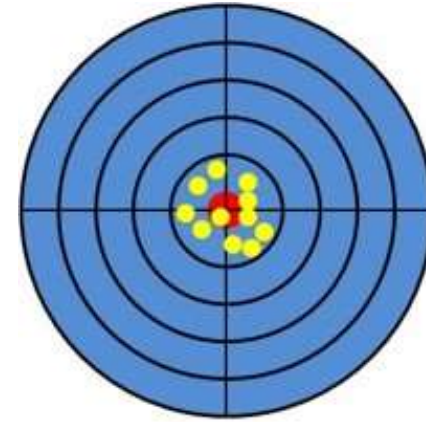
Inaccurate &
Precise



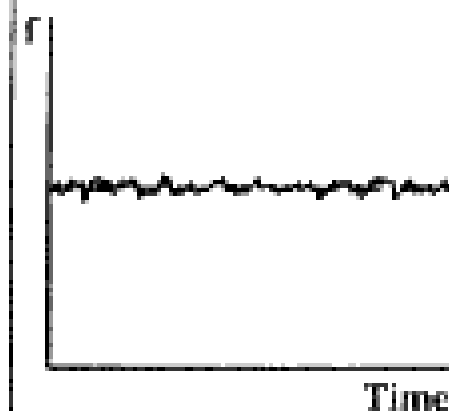
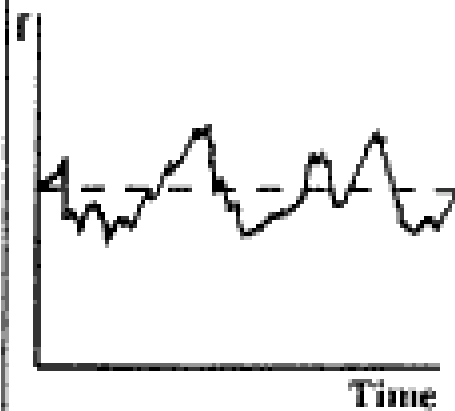
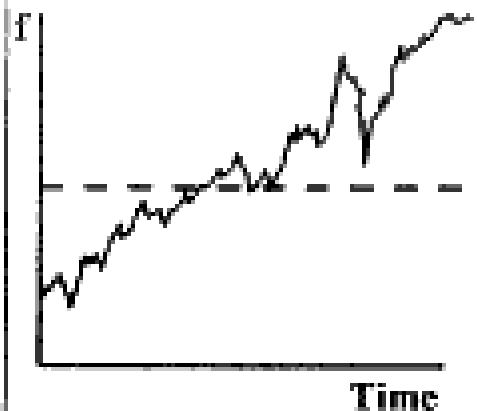
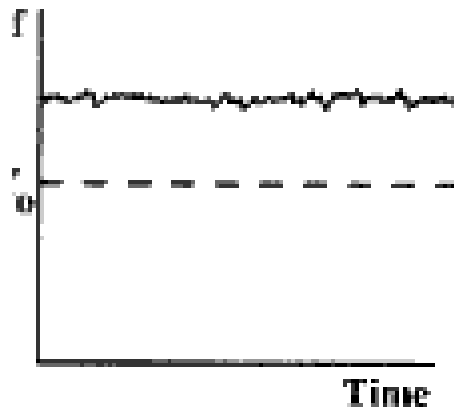
Inaccurate &
Imprecise



Accurate &
Imprecise



Accurate &
Precise



Uncertainty Analysis Process

1. Define the Measurement Process

Identify the Objectives, Calculations, Parameters, Calibrations, Functional Relationships

2. List Elemental Error Sources

Brainstorm all potential sources of error for each component

3. Calculate Systematic and Random Uncertainty

From empirical data or other sources

4. Propagate Standard Deviations

Establish probability curves

5. Data Reduction

Make any necessary adjustments/corrections

6. Calculate Total Uncertainty

Combine and expand

So What Does This Mean To Me?...

- How do I know if what I already have is good enough?
- When should I care and require low uncertainty?
- How sensitive is uncertainty on the measurement of interest?
- What is the point of diminishing returns?



ASHRAE

“Test results should *never* be reported without also reporting their measurement uncertainty. No manager or process owner should take action based on the test results with an undefined measurement uncertainty.”

- Dieck (1992)

You Should Care!

Because...*Garbage In = Garbage Out!*

- ✓ **Performance testing (yes)**
- ✓ **High value decisions (yes)**
- ❖ **Day-to-day operations (not so much)**


Measurement, *tolerance*, confidence

124,582 PPH

+/- 1,000 PPH

95% confidence (k=2)

Uncertainty is the culmination of both *Systematic* and *Random* Uncertainties.



Sources of Uncertainty

Systematic Uncertainty

- Incorrect Installation
- Calibration Error
- Instrument Drift
- Hysteresis
- Flow Stratification
- Environmental Factors
- Electrical Noise

Random Uncertainty

- Instrument Quality
- System Stability
- Environmental Factors

Some Typical Uncertainties

- **Efficiency:**

Packaged Boiler (w/economizer)

- Energy Balance Method
 - 0.2 – 0.5% (gas)
 - 0.3 – 0.6% (oil)
- Input-Output Method
 - 1.2% (gas or oil)

- **Heat Rate**

- Solid Fuel: <3.0%
- All others: <1.5%

- **Power**

- All: <1.0%

Power Plant Example

- Efficiency (Input-Output Method)

$$\eta = \frac{\text{Energy}_{out}}{\text{Energy}_{in}} \times 100$$

$$\eta = \frac{BTU_{Steam} - BTU_{Feedwater}}{BTU_{Fuel}} \times 100$$

$$\eta = \frac{(PPH_{Steam} * h_{g,steam}) - (PPH_{Feedwater} * h_{f,feedwater})}{kcfh * HHV}$$

Power Plant Example

Characteristics	Units	Min Fire	25%	50%	75%	100%
Boiler Master Out	%	12.5	26	50	75	100
Capacity (Steam Flow)	kPPH	26.2	41.5	79.6	116.8	156.7
Outlet Pressure	psig	208.1	207.3	220.7	197.4	225.8
Drum Temperature	F	395	395.4	402.8	399.7	413.8
Drum Pressure	psig	219.1	219.7	240.2	231.6	273.8
Superheat Temperature	F	435.4	451.7	452.7	437.3	440.1
Fuel Flow (NG)	kCFH	23.2	46.1	92.5	138.6	184.4
Fuel Cv Position (Main)	% open	9.00	19.3	36.1	51.3	77.7
Gas Supply Pressure	psig	14.9	15	14.6	14.5	14.3
Main Flame Scanner	-	76	86.8	87	86.8	87
Feedwater Flow	kPPH	19.4	46	73.4	112	148.1
Feedwater Cv Position	% open	10.8	24	40.8	51.5	76.1
FW Entering Econo	F	228	228.5	229	229.2	229.1
FW Exiting Econo	F	252.2	244	249.1	263.2	279.5

Efficiency = 81.4%

Power Plant Example

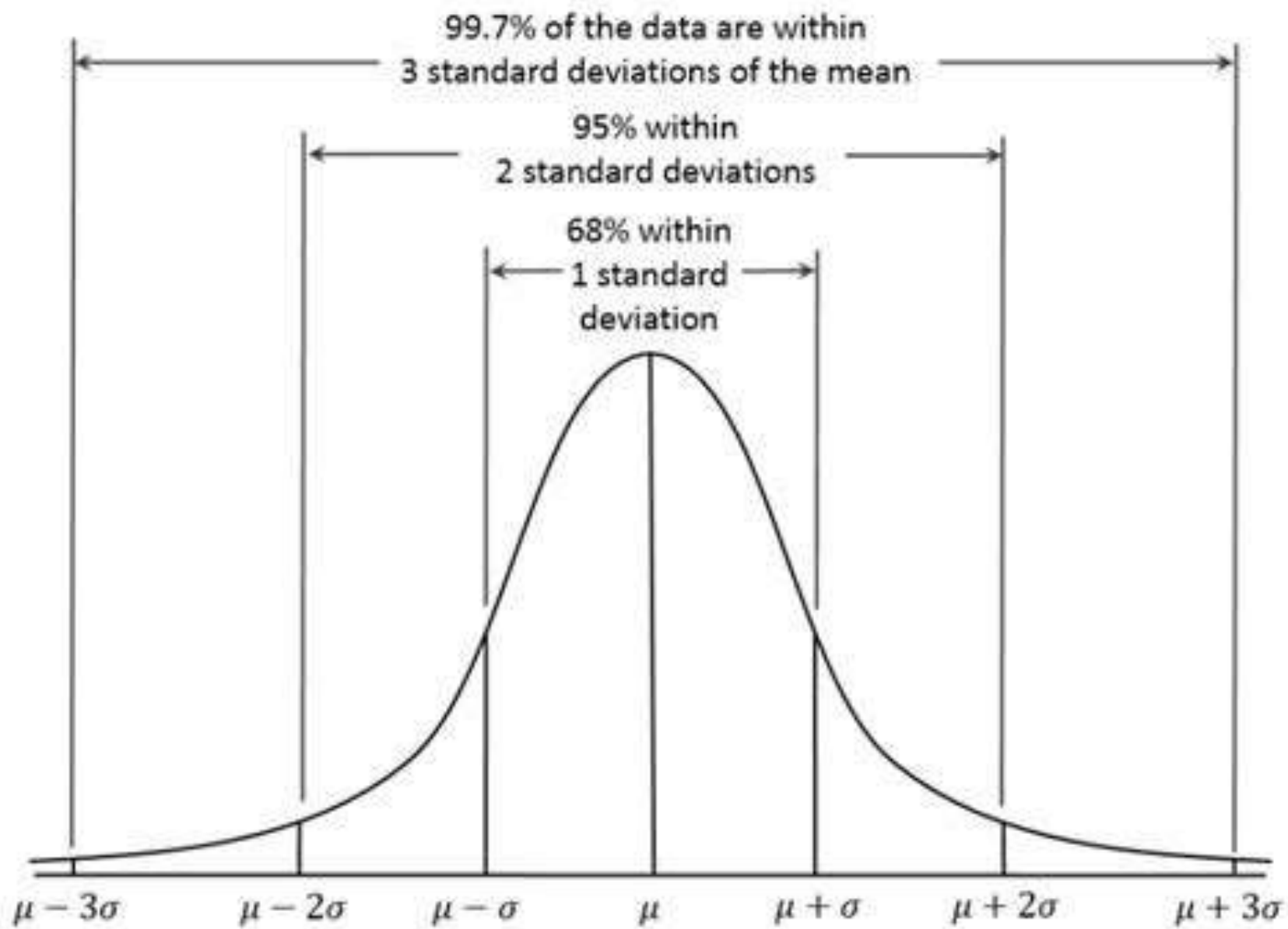
Uncertainty						
Systematic	Random	θ	Systematic Contribution		Random Contribution	
0.50	0.310	1.027	0.263682		0.101359	
0.25	0.500	0	0		0	
0.18	-1.100	0	0		0	
0.25	-0.750	0	0		0	
0.18	1.300	0.217	0.001526		0.07958	
2.00	0.092	-0.787	2.477476		0.005242	
0.50	-0.300	0	0		0	
0.25	0.000	0	0		0	
0.20	-0.250	0	0		0	
2.00	2.600	-0.182	0.132496		0.223918	
0.50	0.200	0	0		0	
0.13	0.030	0	0		0	
0.13	0.060	-0.228	0.000879		0.000187	
			2.49499		0.258406	
	Combined	2.508336	U_R	Expanded	+/- 5.02%	$U_{R,95}$

Power Plant Example

Uncertainty					
Systematic	Random	θ	Systematic Contribution		Random Contribution
0.50	0.310	1.027	0.263682		0.101359
0.25	0.500	0	0		0
0.18	-1.100	0	0		0
0.25	-0.750	0	0		0
0.18	1.300	0.217	0.001526		0.07958
0.50	0.092	-0.787	0.154842		0.005242
0.50	-0.300	0	0		0
0.25	0.000	0	0		0
0.20	-0.250	0	0		0
2.00	2.600	-0.182	0.132496		0.223918
0.50	0.200	0	0		0
0.13	0.030	0	0		0
0.13	0.060	-0.228	0.000879		0.000187
			0.333261		0.258406
	Combined	0.421707	U_R	Expanded	+/- 0.84% $U_{R,95}$

Power Plant Example

Uncertainty					
Systematic	Random	θ	Systematic Contribution		Random Contribution
0.50	0.310	1.027	0.263682		0.101359
0.25	0.500	0	0		0
0.18	-1.100	0	0		0
0.25	-0.750	0	0		0
0.18	1.300	0.217	0.001526		0.07958
0.50	0.092	-0.787	0.154842		0.005242
0.50	-0.300	0	0		0
0.25	0.000	0	0		0
0.20	-0.250	0	0		0
0.50	2.600	-0.182	0.008281		0.223918
0.50	0.200	0	0		0
0.13	0.030	0	0		0
0.13	0.060	-0.228	0.000879		0.000187
			0.305902		0.258406
	Combined	0.400437	U_R	Expanded	+/- 0.80% $U_{R,95}$



Calculating Uncertainty

POWER

- Fundamental: $P_{corr} = (P_{meas} + \sum_{i=1}^7 \Delta_i) \prod_{j=1}^5 \alpha_j$
- Specific: $P_{corr} = (P_{meas} + \Delta_1 + \Delta_2 + \Delta_3 + \Delta_4) \alpha_1 \alpha_2 \alpha_3$

HEAT RATE

- Fundamental: $HR_{corr} = \frac{(Q_{meas} + \sum_{i=1}^7 \omega_i) \prod_{j=1}^5 \beta_j}{(P_{meas} + \sum_{i=1}^7 \Delta_i) \prod_{j=1}^5 \alpha_j}$
- Specific: $HR_{corr} = \frac{(Q_{meas}) \beta_1 \beta_2 \beta_3}{(P_{meas} + \Delta_1 + \Delta_2 + \Delta_3 + \Delta_4) \alpha_1 \alpha_2 \alpha_3}$

Calculating Uncertainty

$$\frac{U_{HR_{corr}}}{HR_{corr}} = \left[\frac{U_{Q_{meas}}^2}{HR_{corr}^2} \left(\frac{\partial HR_{corr}}{\partial Q_{meas}} \right)^2 + \frac{U_{P_{meas}}^2}{HR_{corr}^2} \left(\frac{\partial HR_{corr}}{\partial P_{meas}} \right)^2 + \frac{U_{m_{therm}}^2}{HR_{corr}^2} \left(\frac{\partial HR_{corr}}{\partial m_{therm}} \right)^2 + \frac{U_{pf}^2}{HR_{corr}^2} \left(\frac{\partial HR_{corr}}{\partial pf} \right)^2 + \frac{U_{T_{inl}}^2}{HR_{corr}^2} \left(\frac{\partial HR_{corr}}{\partial T_{inl}} \right)^2 + \frac{U_{P_{amb}}^2}{HR_{corr}^2} \left(\frac{\partial HR_{corr}}{\partial P_{amb}} \right)^2 \right]$$

Metrological Traceability

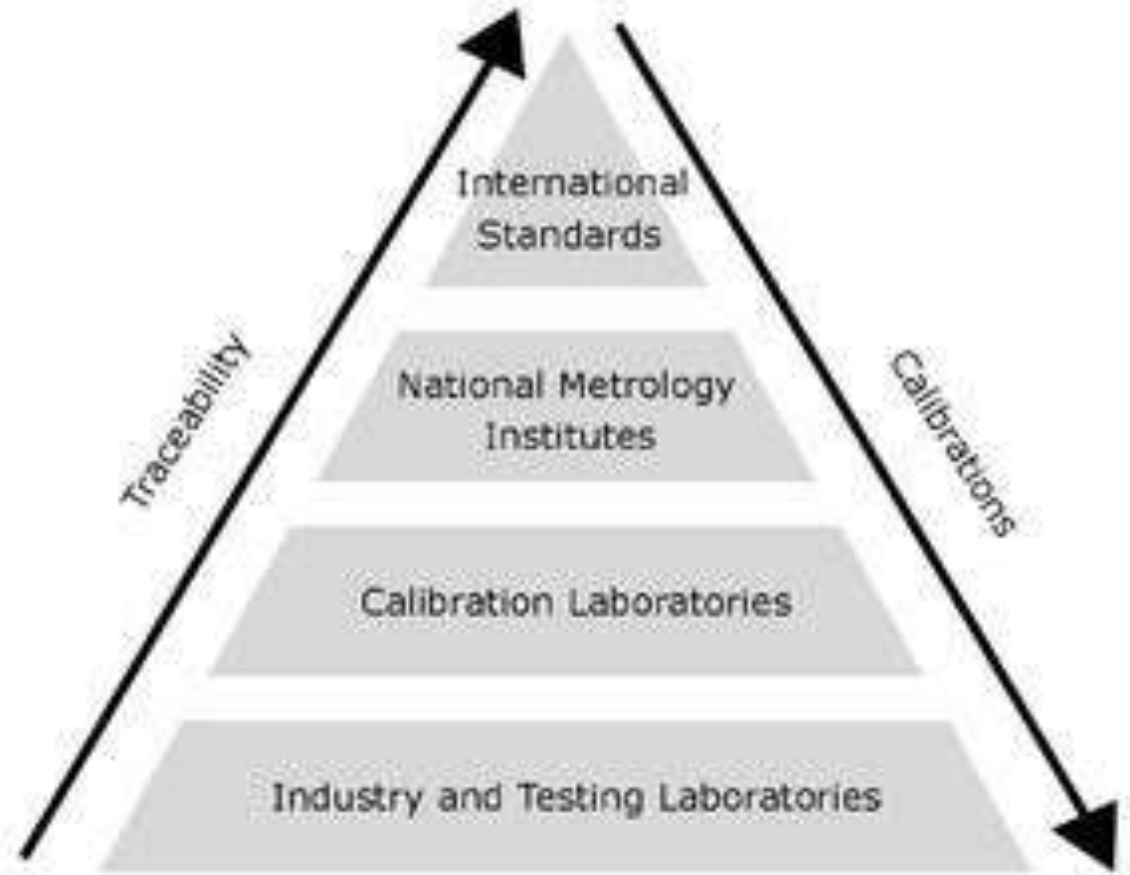
“Property of a measurement result whereby the result can be related to a reference through a documented unbroken chain of calibrations, each contributing to the measurement uncertainty.”

International Vocabulary of Metrology

Basic and General Concepts and Associated Terms, definition 2.41

Traceability

- “NIST Traceability”
- Certificate of Traceability





Conclusion

- Be aware of Measurement Uncertainty.
- Identify where you could be exposed to uncertainty.
- Know how and when to control it.



Brian Wodka, PE, CxA, CEM, LEED AP

RMF Engineering

IDEA CampusEnergy2019

References:

ASME PTC 4 “Fired Steam Generators”

ASME PTC 19.2 “Test Uncertainty”

ASME PTC 46 “Overall Plant Performance”

JCGM 200:2008 “Vocabulaire International de Metrologie” (VIM)

JCGM 100:2008 “Guide to the Expression of Uncertainty in Measurement” (GUM)

ASHRAE 150 “Thermal Storage Performance Test Procedure”

www.nist.gov